Reservoir Simulation Homework #1 a.kariman1990@gmail.com

1. Prove that:

$$\frac{df}{dx} = \frac{-f_{i+2} + 4f_{i+1} - 3f_{i}}{2h} + O(h^{2})$$

$$\frac{df}{dx} = \frac{8(f_{i+1} - f_{i-1}) - (f_{i+2} - f_{i-2})}{12h} + O(h^{4})$$

2. Obtain the flow equation of compressible fluids using P^2 -method and Pseudo-Pressure approach:

$$\frac{\varphi \mu_{g} c_{g}}{k} \frac{\partial p^{2}}{\partial t} = \nabla^{2} p^{2} + \frac{2zRT \mu_{g}}{Wk} q$$

$$\frac{\varphi \mu_{g} c_{g}}{k} \frac{\partial \psi}{\partial t} = \nabla^{2} \psi + \frac{2RT}{Wk} q$$

Where the W is the molecular weight of gas, z is compressibility factor, R is the universal gas constant and k is the permeability of porous media.

3. Drive the single phase flow equation for slightly compressible fluid in cylindrical geometry.